# Package: ClusROC (via r-universe)

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Type Package Title ROC Analysis in Three-Class Classification Problems for Clustered Data Date 2022-11-17 Version 1.0.2 Author Duc-Khanh To [aut, cre] (<https://orcid.org/0000-0002-4641-0764>), with contributions from Gianfranco Adimari and Monica Chiogna Maintainer Duc-Khanh To <toduc@stat.unipd.it> **Description** Statistical methods for ROC surface analysis in three-class classification problems for clustered data and in presence of covariates. In particular, the package allows to obtain covariate-specific point and interval estimation for: (i) true class fractions (TCFs) at fixed pairs of thresholds; (ii) the ROC surface; (iii) the volume under ROC surface (VUS); (iv) the optimal pairs of thresholds. Methods considered in points (i), (ii) and (iv) are proposed and discussed in To et al. (2022) <doi:10.1177/09622802221089029>. Referring to point (iv), three different selection criteria are implemented: Generalized Youden Index (GYI), Closest to Perfection (CtP) and Maximum Volume (MV). Methods considered in point (iii) are proposed and discussed in Xiong et al. (2018) <doi:10.1177/0962280217742539>. Visualization tools are also provided. We refer readers to the articles cited above for all details.

# License GPL-3

**Depends** R (>= 3.5.0), stats, utils, graphics, nlme, Rcpp (>= 0.12.3)

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# Contents

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# Contents

ClusROC-package
ci_clus_vus
clus_lme
clus_opt_thres3
clus_roc_surface
clus_tcfs
clus_vus
data_3class
data_3class_bcx
EnergyEthiopia 17
MouseNeurons
plot.clus_lme
plot.clus_opt_thres3
print.ci_clus_vus
print.clus_lme
print.clus_opt_thres3
print.clus_tcfs
print.clus_vus

# Index

2

ClusROC-package

ROC Analysis in Three-Class Classification Problems for Clustered Data

# Description

This package implements the techniques for ROC surface analysis, in cases of clustered data and in presence of covariates. In particular, the package allows to obtain covariate-specific point and interval estimation for: (i) true class fractions (TCFs) at fixed pairs of thresholds; (ii) the ROC surface; (iii) the volume under ROC surface (VUS); (iv) the optimal pairs of thresholds. Methods considered in points (i), (ii) and (iv) are proposed and discussed in To et al. (2022). Referring to point (iv), three different selection criteria are implemented: Generalized Youden Index (GYI), Closest to Perfection (CtP) and Maximum Volume (MV). Methods considered in point (iii) are proposed and discussed in Xiong et al. (2018). Visualization tools are also provided. We refer readers to the articles cited above for all details.

#### Details

Package:	ClusROC
Type:	Package
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License:	GPL 2   GPL 3
Lazy load:	yes

Major functions are clus\_lme, clus\_roc\_surface, clus\_opt\_thres3, clus\_vus and clus\_tcfs.

#### Author(s)

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#### References

Bantis, L. E., Nakas, C. T., Reiser, B., Myall, D., and Dalrymple-Alford, J. C. (2017). Construction of joint confidence regions for the optimal true class fractions of Receiver Operating Characteristic (ROC) surfaces and manifolds. *Statistical methods in medical research*, **26**, 3, 1429-1442.

Gurka, M. J., Edwards, L. J., Muller, K. E., and Kupper, L. L. (2006). Extending the Box-Cox transformation to the linear mixed model. *Journal of the Royal Statistical Society: Series A (Statistics in Society)*, **169**, 2, 273-288.

Gurka, M. J. and Edwards, L. J. (2011). Estimating variance components and random effects using the box-cox transformation in the linear mixed model. *Communications in Statistics - Theory and Methods*, **40**, 3, 515-531.

Kauermann, G. and Carroll, R. J. (2001). A note on the efficiency of sandwich covariance matrix estimation. *Journal of the American Statistical Association*, **96**, 456, 1387-1396.

Liang, K. Y. and Zeger, S. L. (1986). Longitudinal data analysis using generalized linear models. *Biometrika*, **73**, 1, 13-22.

Mancl, L. A. and DeRouen, T. A. (2001). A covariance estimator for GEE with improved smallsample properties. *Biometrics*, **57**, 1, 126-134.

To, D-K., Adimari, G., Chiogna, M. and Risso, D. (2022). Receiver operating characteristic estimation and threshold selection criteria in three-class classification problems for clustered data. *Statistical Methods in Medical Research*, **7**, 31, 1325-1341.

Xiong, C., Luo, J., Chen L., Gao, F., Liu, J., Wang, G., Bateman, R. and Morris, J. C. (2018). Estimating diagnostic accuracy for clustered ordinal diagnostic groups in the three-class case – Application to the early diagnosis of Alzheimer disease. *Statistical Methods in Medical Research*, **27**, 3, 701-714.

ci\_clus\_vus

Confidence Intervals for Covariate-specific VUS

#### Description

Computes confidence intervals for covariate-specific VUS.

#### Usage

ci\_clus\_vus(x, ci\_level = 0.95)

#### Arguments

Х	an object of class "VUS", a result of clus_vus call.
ci_level	a confidence level to be used for constructing the confidence interval; default is 0.95.

#### Details

A confidence interval for covariate-specific VUS is given based on normal approximation. If the lower bound (or the upper bound) of the confidence interval is smaller than 0 (or greater than 1), it will be set as 0 (or 1). Also, logit and probit transformations are available if one wants guarantees that confidence limits are inside (0, 1).

#### Value

ci\_clus\_vus returns an object of class inheriting from "ci\_VUS" class. An object of class "ci\_VUS" is a list, containing at least the following components:

ci_vus_norm	the normal approximation-based confidence interval for covariate-specific VUS.
ci_vus_log	the confidence interval for covariate-specific VUS, after using logit-transformation.
ci_vus_prob	the confidence interval for covariate-specific VUS, after using probit-transformation.

4

# clus\_lme

ci_level	fixed confidence level.
newdata	value(s) of covariate(s).
n_p	total numbers of the regressors in the model.

# See Also

clus\_vus

clus_lme	Linear Mixed-Effects Models for a continuous diagnostic test or a
	biomarker (or a classifier).

# Description

clus\_lme fits the cluster-effect model for a continuous diagnostic test in a three-class setting as described in Xiong et al. (2018) and To et al. (2022).

# Usage

```
clus_lme(
  fixed_formula,
  name_class,
  name_clust,
  data = sys.frame(sys.parent()),
  subset,
  na_action = na.fail,
  levl_class = NULL,
  ap_var = TRUE,
  boxcox = FALSE,
  interval_lambda = c(-2, 2),
  trace = TRUE,
  ...
)
```

# Arguments

fixed_formula	a two-sided linear formula object, describing the fixed-effects part of the model for three classes, with the response on the left of ~ operator and the terms, separated by + operators, on the right. For example, $Y \sim X1 + X2$ , $Y \sim X1 + X2 + X1 : X2$ or $log(Y) \sim X1 + X2 + I(X1^2)$ .
name_class	name of variable indicating three classes (or three groups) in the data.
name_clust	name of variable indicating clusters in the data.
data	a data frame containing the variables in the model.
subset	an optional expression indicating the subset of the rows of data that should be used in the fit. This can be a logical vector, or a numeric vector indicating which observation numbers are to be included, or a character vector of the row names to be included. All observations are included by default.

na_action	a function that indicates what should happen when the data contain NAs. The default action (na.fail) causes clus_lme to print an error message and terminate if there are any incomplete observations.	
levl_class	a vector (of strings) containing the ordered name chosen for the disease classes. The ordering is intended to be "increasing" with respect to the disease severity. If levl_class = NULL (default), the elements of the vector will be automatically determined from data, by considering the order of the means of the test values for each disease class (diagnostic group).	
ap_var	a logical value. Default = TRUE. If set to TRUE, the estimated covariance matrix for all estimated parameters in the model will be obtained (by using the sandwich formula).	
boxcox	a logical value. Default = FALSE. If set to TRUE, a Box-Cox transformation will be applied to the model.	
interval_lambda		
	a vector containing the end-points of the interval for searching the Box-Cox parameter, lambda. Default = $(-2, 2)$ .	
trace	a logical value. Default = TRUE. If set to TRUE, the information about the check for the monotonic ordering of test values will be provided.	
	additional arguments for lme, such as control, contrasts.	

#### Details

This function fits a linear mixed-effect model for a continuous diagnostic test in a three-class setting in order to account for the cluster and covariates effects on the test result. See Xiong et al. (2018) and To et al. (2022) for more details.

- Estimation is done by using lme with the restricted maximum log-likelihood (REML) method.
- Box-Cox transformation for the model can be used when the distributions of test results are skewed (Gurka et al. 2006). The estimation procedure is described in To et al. (2022). The Box-Cox parameter  $\lambda$  is estimated by a grid search on the interval (-2, 2), as discussed in Gurka and Edwards (2011).
- The estimated variance-covariance matrix for the estimated parameters are obtained by sandwich formula (see, Liang and Zeger, 1986; Kauermann and Carroll, 2001; Mancl and DeRouen, 2001) as discussed in To et al. (2022).

#### Value

clus\_lme returns an object of class "clus\_lme" class, i.e., a list containing at least the following components:

call	the matched call.
est_para	a vector containing the estimated parameters.
se_para	a vector containing the standard errors.
vcov_sand	the estimated covariance matrix for all estimated parameters.
residual	a list of residuals.
fitted	a list of fitted values.

randf	a vector of estimated random effects for each cluster level.
n_coef	total number of coefficients included in the model.
n_p	total numbers of regressors in the model.
icc	an estimate of intra-class correlation - ICC
terms	the terms object used.
boxcox	logical value indicating whether the Box-Cox transformation was applied or not.
data	data frame is used to fitting model.

Generic functions such as print and plot are also used to show results of the fit.

#### References

Gurka, M. J., Edwards, L. J., Muller, K. E., and Kupper, L. L. (2006) "Extending the Box-Cox transformation to the linear mixed model". *Journal of the Royal Statistical Society: Series A (Statistics in Society)*, **169**, 2, 273-288.

Gurka, M. J. and Edwards, L. J. (2011) "Estimating variance components and random effects using the box-cox transformation in the linear mixed model". *Communications in Statistics - Theory and Methods*, **40**, 3, 515-531.

Kauermann, G. and Carroll, R. J. (2001) "A note on the efficiency of sandwich covariance matrix estimation". *Journal of the American Statistical Association*, **96**, 456, 1387-1396.

Liang, K. Y. and Zeger, S. L. (1986) "Longitudinal data analysis using generalized linear models". *Biometrika*, **73**, 1, 13-22.

Mancl, L. A. and DeRouen, T. A. (2001) "A covariance estimator for GEE with improved small-sample properties". *Biometrics*, **57**, 1, 126-134.

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Xiong, C., Luo, J., Chen L., Gao, F., Liu, J., Wang, G., Bateman, R. and Morris, J. C. (2018) "Estimating diagnostic accuracy for clustered ordinal diagnostic groups in the three-class case – Application to the early diagnosis of Alzheimer disease". *Statistical Methods in Medical Research*, **27**, 3, 701-714.

#### Examples

## Example 2: Box-Cox transformation
data(data\_3class\_bcx)

clus_opt_thres3	Estimation of the covariate-specific optimal pair of thresholds for clus-
	tered data.

#### Description

clus\_opt\_thres3 estimates covariate-specific optimal pair of thresholds of a continuous diagnostic test in a clustered design, with three classes of diseases.

#### Usage

```
clus_opt_thres3(
  method = c("GYI", "CtP", "MV"),
  out_clus_lme,
  newdata,
  ap_var = TRUE,
  control = list()
)
```

#### Arguments

method	the method to be used. See 'Details'.
out_clus_lme	an object of class "clus_lme", i.e., a result of clus_lme call.
newdata	a data frame (containing specific value(s) of covariate(s)) in which to look for variables with which to estimate covariate-specific optimal pair of thresholds. In absence of covariate, no values have to be specified.
ap_var	logical value. If set to TRUE, the variance-covariance matrix of (estimated) covariate-specific optimal thresholds is estimated.
control	a list of control parameters. See 'Details'.

# Details

This function implements estimation methods discussed in To et al. (2022) for covariate-specific optimal pair of thresholds in a clustered design with three ordinal groups. The estimators are based on the results from clus\_lme function, which fits the linear mixed-effect model by using REML approach.

Before performing estimation, a check for the monotone ordering assumption is performed. This means that, for the fixed values of covariates, three predicted mean values for test results in three

diagnostic groups are compared. If the assumption is not meet, the covariate-specific optimal pair of thresholds at the values of covariates are not estimated.

The estimation procedure uses three criteria. Method "GYI" is Generalized Youden Index, which maximizes the sum of three covariate-specific True Class Fractions - TCFs. Method "CtP" is based on Closest to Pefection approach. By using this method, the optimal pair of thresholds is obtained by minimizing the distance, in the unit cube, between a generic point on the covariate-specific ROC surface and the top corner (1, 1, 1). Method "MV" is based on Maximum Volume approach, which searches for thresholds that maximize the volume of a box under the covariate-specific ROC surface. The user can select more than one method. This function allows to estimate covariate-specific optimal pair of thresholds at multiple points for covariates.

The asymptotic variance-covariance matrix of the (estimated) covariate-specific optimal thresholds is estimated by using the Delta method under the normal assumption. If the Box-Cox transformation is applied to the linear mixed-effect model, a nonparametric bootstrap procedure for clustered data will be used to obtain the estimated asymptotic covariance matrix (see To et al. 2022, for more details).

The control argument is a list that can supply any of the following components:

- method\_optim Optimization method to be used. There are three options: "L-BFGS-B", "BFGS" and "Nelder-Mead". Default is "L-BFGS-B".
- start Starting values in the optimization procedure. If it is NULL, a starting point will be automatically obtained.
- maxit The maximum number of iterations. Default is 200.
- lower, upper Possible bounds on the threshold range, for the optimization based on "L-BFGS-B" method. Defaults are -Inf and Inf.
- n\_boot Number of bootstrap replicates for estimating the covariance matrix (when Box-Cox transformation is applied). Default is 250.
- parallel A logical value. If set to TRUE, a parallel computing is employed in the bootstrap resampling process.

ncpus Number of processes to be used in parallel computing. Default is 2.

#### Value

clus\_opt\_thres3 returns an object of "clus\_opt\_thres3" class, which is a list containing at least the following components:

call	the matched call.
method	the methods used to obtain the estimated optimal pair of threholds.
thres3	a vector or matrix containing the estimated optimal thresholds.
thres3_se	a vector or matrix containing the estimated standard errors.
vcov_thres3	a matrix or list of matrices containing the estimated variance-covariance matri-
	ces.
tcfs	a vector or matrix containing the estimated TCFs at the optimal thresholds.
mess_order	a diagnostic message from checking the monontone ordering.
newdata	value(s) of covariate(s).
n_p	total number of regressors in the model.

Generic functions such as print and plot are also used to show the results.

#### References

To, D-K., Adimari, G., Chiogna, M. and Risso, D. (2022) "Receiver operating characteristic estimation and threshold selection criteria in three-class classification problems for clustered data". *Statistical Methods in Medical Research*, **7**, 31, 1325-1341.

#### Examples

```
data(data_3class)
## One covariate
out1 <- clus_lme(fixed_formula = Y ~ X1, name_class = "D",</pre>
                 name_clust = "id_Clus", data = data_3class)
### Estimate covariate-specific optimal thresholds at multiple values of one covariate,
### with 3 methods
out_thres_1 <- clus_opt_thres3(method = c("GYI", "MV", "CtP"),</pre>
                                out_clus_lme = out1,
                                newdata = data.frame(X1 = 1), ap_var = TRUE)
print(out_thres_1)
plot(out_thres_1)
## Two covariates
out2 <- clus_lme(fixed_formula = Y ~ X1 + X2, name_class = "D",</pre>
                 name_clust = "id_Clus", data = data_3class)
### Estimate covariate-specific optimal thresholds at one point, with 3 methods
out_thres_2 <- clus_opt_thres3(method = c("GYI", "MV", "CtP"),</pre>
                                out_clus_lme = out2,
                                newdata = data.frame(X1 = 1, X2 = 0),
                                ap_var = TRUE)
print(out_thres_2)
plot(out_thres_2)
### Estimate covariate-specific optimal thresholds at three points, with 3 methods
out_thres_3 <- clus_opt_thres3(method = c("GYI", "MV", "CtP"),</pre>
                                out_clus_lme = out2,
                                newdata = data.frame(X1 = c(-0.5, 0.5, 0.5),
                                                      X2 = c(0, 0, 1)),
                                ap_var = TRUE)
print(out_thres_3)
plot(out_thres_3, colors = c("forestgreen", "blue"))
```

clus\_roc\_surface Plot an estimated covariate-specific ROC surface for clustered data.

#### Description

clus\_roc\_surface estimates and makes a 3D plot of a covariate-specific ROC surface for a continuous diagnostic test, in a clustered design, with three ordinal groups. clus\_roc\_surface

# Usage

```
clus_roc_surface(
  out_clus_lme,
  newdata,
  step_tcf = 0.01,
  main = NULL,
  file_name = NULL,
  ellips = FALSE,
  thresholds = NULL,
  ci_level = ifelse(ellips, 0.95, NULL)
)
```

# Arguments

<pre>out_clus_lme</pre>	an object of class "clus_lme", a result of clus_lme call.
newdata	a data frame with 1 row (containing specific value(s) of covariate(s)) in which to look for variables with which to estimate covariate-specific ROC. In absence of covariate, no values have to be specified.
<pre>step_tcf</pre>	number: increment to be used in the grid for $p1 = tcf1$ and $p3 = tcf3$ .
main	the main title for plot.
file_name	File name to create on disk.
ellips	a logical value. If set to TRUE, the function adds an ellipsoidal confidence region for TCFs (True Class Fractions), at a specified pair of values for the thresholds, to the plot of estimated covariate-specific ROC surface.
thresholds	a specified pair of thresholds, used to construct the ellipsoidal confidence region for TCFs.
ci_level	a confidence level to be used for constructing the ellipsoidal confidence region; default is 0.95.

# Details

This function implements a method in To et al. (2022) for estimating covariate-specific ROC surface of a continuous diagnostic test in a clustered design, with three ordinal groups. The estimator is based on the results from clus\_lme with REML approach.

Before performing estimation, a check for the monotone ordering assumption is performed. This means that, for the fixed values of covariates, three predicted mean values for test results in three diagnostic groups are compared. If the assumption is not meet, the covariate-specific ROC surface at the values of covariates is not estimated.

The ellipsoidal confidence region for TCFs at a given pair of thresholds, if required, is constructed by using normal approximation and is plotted in the ROC surface space. The confidence level (default) is 0.95. Note that, if the Box-Cox transformation is applied for the linear mixed-effect model, the pair of thresholds must be input in the original scale. If the constructed confidence region for TCFs is outside the unit cube, a probit transformation will be automatically applied to obtain an appropriate confidence region, which is inside the unit cube (see Bantis et. al., 2017).

#### Value

clus\_roc\_surface returns a 3D rgl plot of the estimated covariate-specific ROC surface.

# References

Bantis, L. E., Nakas, C. T., Reiser, B., Myall, D., and Dalrymple-Alford, J. C. (2017). "Construction of joint confidence regions for the optimal true class fractions of Receiver Operating Characteristic (ROC) surfaces and manifolds". *Statistical methods in medical research*, **26**, 3, 1429-1442.

To, D-K., Adimari, G., Chiogna, M. and Risso, D. (2022) "Receiver operating characteristic estimation and threshold selection criteria in three-class classification problems for clustered data". *Statistical Methods in Medical Research*, **7**, 31, 1325-1341.

#### Examples

```
data(data_3class)
## One covariate
out1 <- clus_lme(fixed_formula = Y ~ X1, name_class = "D",</pre>
                 name_clust = "id_Clus", data = data_3class)
### plot only covariate-specific ROC surface
clus_roc_surface(out_clus_lme = out1, newdata = data.frame(X1 = 1))
### plot covariate-specific ROC surface and a 95% ellipsoidal confidence region for TCFs
clus_roc_surface(out_clus_lme = out1, newdata = data.frame(X1 = 1),
                 ellips = TRUE, thresholds = c(0.9, 3.95))
## Two covariates
out2 <- clus_lme(fixed_formula = Y ~ X1 + X2, name_class = "D",</pre>
                 name_clust = "id_Clus", data = data_3class)
### plot only covariate-specific ROC surface
clus_roc_surface(out_clus_lme = out2, newdata = data.frame(X1 = 1, X2 = 1))
### plot covariate-specific ROC surface and a 95% ellipsoidal confidence region for TCFs
clus_roc_surface(out_clus_lme = out2, newdata = data.frame(X1 = 1, X2 = 1),
                 ellips = TRUE, thresholds = c(0.9, 3.95))
```

clus\_tcfs

Estimation of the covariate-specific TCFs for clustered data.

#### Description

clus\_tcfs estimates covariate-specific True Class Fractions (TCFs), at a specified pair of thresholds, of a continuous diagnostic test in a clustered design with three ordinal groups. This function allows to estimate covariate-specific TCFs at multiple points for covariates.

#### clus\_tcfs

# Usage

clus\_tcfs(out\_clus\_lme, newdata, thresholds, ap\_var = FALSE)

#### Arguments

<pre>out_clus_lme</pre>	an object of class "clus_lme", a result of clus_lme call.
newdata	a data frame (containing specific value(s) of covariate(s)) in which to look for variables with which to estimate covariate-specific TCFs. In absence of covariate, no values have to be specified.
thresholds	a specified pair of thresholds.
ap_var	logical value. If set to TRUE, the variance-covariance matrix of estimated covariate-specific TCFs is estimated.

#### Details

This function implements a method in To et al. (2022) for estimating covariate-specific TCFs at a specified pair of thresholds of a continuous diagnostic test in a clustered design with three ordinal groups. The estimator is based on results from clus\_lme, which uses the REML approach. The asymptotic variance-covariance matrix of the estimated covariate-specific TCFs is estimated through the Delta method. Note that, if the Box-Cox transformation is applied for the linear mixed-effect model, the pair of thresholds must be input in the original scale.

Before performing estimation, a check for the monotone ordering assumption is performed. This means that, for the fixed values of covariates, three predicted mean values for test results in three diagnostic groups are compared. If the assumption is not meet, the covariate-specific TCFs at the values of covariates are not estimated.

#### Value

TCFs returns an object of class "TCFs", which is a list containing at least the following components:

call	the matched call.
tcfs_est	a vector or matrix containing the estimated TCFs.
tcf_vcov	a matrix or list of matrices containing the estimated variance-covariance matrices.
thresholds	specified pair of thresholds.
mess_order	a diagnostic message from checking the monontone ordering.
newdata	value(s) of covariate(s).
n_p	total number of regressors in the model.

Generic functions such as print is also used to show the results.

# References

To, D-K., Adimari, G., Chiogna, M. and Risso, D. (2022) "Receiver operating characteristic estimation and threshold selection criteria in three-class classification problems for clustered data". *Statistical Methods in Medical Research*, **7**, 31, 1325-1341.

# Examples

```
data(data_3class)
## One covariate
out1 <- clus_lme(fixed_formula = Y ~ X1, name_class = "D",</pre>
                 name_clust = "id_Clus", data = data_3class)
### Estimate TCFs at one single value of X1, (t1, t2) = (1, 4)
out_tcfs_1 <- clus_tcfs(out_clus_lme = out1, newdata = data.frame(X1 = 1),</pre>
                         thresholds = c(1, 4), ap_var = TRUE)
print(out_tcfs_1)
## Two covariates
out2 <- clus_lme(fixed_formula = Y ~ X1 + X2, name_class = "D",</pre>
                 name_clust = "id_Clus", data = data_3class)
### Estimate covariate-specific TCFs at point (X1, X2) = (1, 0), and (t1, t2) = (1, 4)
out_tcfs_2 <- clus_tcfs(out_clus_lme = out2,</pre>
                         newdata = data.frame(X1 = 1, X2 = 0),
                         thresholds = c(1, 4), ap_var = TRUE)
print(out_tcfs_2)
### Estimate covariate-specific TCFs at three points and (t1, t2) = (1, 4)
out_tcfs_3 <- clus_tcfs(out_clus_lme = out2,</pre>
                         newdata = data.frame(X1 = c(-0.5, 0.5, 0.5),
                                               X2 = c(0, 0, 1)),
                         thresholds = c(1, 4), ap_var = TRUE)
print(out_tcfs_3)
```

clus\_vus

Estimation of the covariate-specific VUS for clustered data.

# Description

This function estimates the covariate-specific VUS of a continuous diagnostic test in the setting of clustered data as described in Xiong et al. (2018). This function allows to estimate covariate-specific VUS at multiple points for covariates.

#### Usage

```
clus_vus(out_clus_lme, newdata, ap_var = TRUE, subdivisions = 1000, ...)
```

# Arguments

<pre>out_clus_lme</pre>	an object of class "clus_lme", a result of clus_lme call.
newdata	a data frame (containing specific value(s) of covariate(s)) in which to look for variables with which to estimate covariate-specific VUS. In absence of covariate, no values have to be specified.

14

#### clus\_vus

ap_var	logical value. If set to TRUE (default), the standard error for (estimated) covariate-specific VUS are estimated.
subdivisions	the maximum number of subintervals used to approximate integral. Default is 1000.
	additional arguments to be passed to integrate.

# Details

This function implements a method in Xiong et al. (2018) for estimating covariate-specific VUS of a continuous diagnostic test in a clustered design with three ordinal groups. The estimator is based on results from clus\_lme, which uses the REML approach. The standard error of the estimated covariate-specific VUS is approximated through the Delta method.

Before performing estimation, a check for the monotone ordering assumption is performed. This means that, for the fixed values of covariates, three predicted mean values for test results in three diagnostic groups are compared. If the assumption is not meet, the covariate-specific VUS at the values of covariates are not estimated. In addition, this function also performs the statistical test,  $H_0: VUS = 1/6$  versus an alternative of interest.

#### Value

clus\_vus returns an object of class "VUS" which is a list containing at least the following components:

call	the matched call.
vus_est	a vector containing the estimated covariate-specific VUS.
vus_se	a vector containing the standard errors.
mess_order	a diagnostic message from checking the monontone ordering.
newdata	value(s) of covariate(s).
n_p	total number of regressors in the model.

Generic functions such as print is also used to show the results.

#### References

Xiong, C., Luo, J., Chen L., Gao, F., Liu, J., Wang, G., Bateman, R. and Morris, J. C. (2018) "Estimating diagnostic accuracy for clustered ordinal diagnostic groups in the three-class case – Application to the early diagnosis of Alzheimer disease". *Statistical Methods in Medical Research*, **27**, 3, 701-714.

#### Examples

### Estimate covariate-specific VUS at one value of one covariate
out\_vus1 <- clus\_vus(out1, newdata = data.frame(X1 = 0.5))</pre>

A simulated data

data\_3class

#### Description

A simulated data example with 30 clusters.

#### Usage

data(data\_3class)

#### Format

A data frame with 225 observations (from 30 clusters).

- id\_Clus the id number of cluster.
- Y a vector containing test results.
- D a factor with 3 levels for the disease status, 1, 2, 3. The levels correspond to benign disease, early stage and late stage.
- X1 a continuous covariate.
- X2 a binary covariate.

#### Description

A simulated data example with 60 clusters. This dataset is used in a example of analysis with Box-Cox transformation.

#### Usage

```
data(data_3class_bcx)
```

#### Format

A data frame with 582 observations (from 60 clusters).

- id\_Clus the id number of cluster.
- Y a vector containing test results.
- D a factor with 3 levels for disease status, 1, 2, 3. The levels correspond to benign disease, early stage and late stage.
- X a continuous covariate.

EnergyEthiopia A subset of energy choice data in 4 cities of Ethiopia

# Description

A subset of energy choice data used in Alem et al. (2016). The authors are used the full dataset to investigate the determinants of household cooking fuel choice and energy transition in urban Ethiopia. A full data is publicly available at doi:10.1016/j.eneco.2016.06.025.

#### Usage

```
data(EnergyEthiopia)
```

#### Format

A data frame with 2088 observations from 1123 households (or clusters) in the capital Addis Ababa and 9 variables:

uqid the id of household (which yield 1123 clusters).

energy2 a factor with 3 levels (types) of cooking energy state at each time (2000, 2004, 2009), i.e., 1 (clean fuel only - electricity, gas and kerosene), 2 (a mix of clean and biomass), 3 (biomass fuel only - firewood, charcoal, dung and crop residues).

hhs household size.

hhs\_ft a factor with 4 levels of household size: small  $(1 \le hhs \le 4)$ ; medium  $(5 \le hhs \le 8)$ ; large  $((9 \le hhs \le 12))$ ; very large (hhs  $\ge 13$ ).

1rconsaeu log of real consumption per adult equivalent units.

lfirewood\_pr Firewood log price.

lcharcol\_pr Charcoal log price.

lkerosene\_pr Kernosene log price.

lelectric\_pr Electricity log price.

# References

Alem, Y., Beyene, A. D., Köhlin, G., & Mekonnen, A. (2016). "Modeling household cooking fuel choice: A panel multinomial logit approach". *Energy Economics*, **59**, 129-137.

MouseNeurons A subset of mouse brain cells data

#### Description

A subset of mouse brain cells data used in To el al. (2022). This is used to evaluate the ability of Lamp5 gene to discriminate three types of glutamatergic neurons. A full data is publicly available at https://portal.brain-map.org/atlases-and-data/rnaseq/mouse-v1-and-alm-smart-seq.

### Usage

data(MouseNeurons)

#### Format

A data frame with 860 observations from 23 clusters and 7 variables:

sample\_name name of each observation.

subclass\_label a factor with 3 levels (types) of glutamatergic neurons, i.e., L2/3 IT (Layer 2/3 Intratelencephalic), L4 (Layer 4) and L5 PT (Layer 5 Pyramidal Tract) neurons.

genotype\_id the mouse genotype (which yield 23 clusters).

sex the gender of mouse.

age\_days the age of mouse, in days.

- Slc17a7\_cpm count per million of Slc17a7 (Solute Carrier Family 17 Member 7) gene expression.
- Lamp5\_cpm count per million of Lamp5 (Lysosomal Associated Membrane Protein Family Member 5) gene expression.

#### References

To, D-K., Adimari, G., Chiogna, M. and Risso, D. (2022) "Receiver operating characteristic estimation and threshold selection criteria in three-class classification problems for clustered data". *Statistical Methods in Medical Research*, **7**, 31, 1325-1341. plot.clus\_lme Plot an clus\_lme object.

#### Description

Diagnostic plots for the linear mixed-effect model, fitted by clus\_lme.

#### Usage

```
## S3 method for class 'clus_lme'
plot(x, file_name = NULL, ...)
```

# Arguments

х	an object of class "clus_lme", i.e., a result of clus_lme call.
file_name	File name to create on disk.
	further arguments used with ggexport function, for example, width, height.

# Details

plot.clus\_lme provides three diagnostic plots: Q-Q plots for residuals, Fitted vs. Residuals values, and Q-Q plot for cluster effects, based on ggplot().

# Value

plot.clus\_lme returns the diagnostic plots for the linear mixed-effect model, fitted by clus\_lme.

#### See Also

clus\_lme

plot.clus\_opt\_thres3 *Plot of confidence regions for covariate-specific optimal pair of thresholds.* 

# Description

This function plots confidence regions for covariate-specific optimal pair of thresholds.

# Usage

```
## S3 method for class 'clus_opt_thres3'
plot(
    x,
    ci_level = 0.95,
    colors = NULL,
    xlims,
    ylims,
    size_point = 0.5,
    size_path = 0.5,
    names_labels,
    nrow_legend = 1,
    file_name = NULL,
    ...
)
```

# Arguments

x	an object of class "clus_opt_thres3", i.e., a result of clus_opt_thres3.	
ci_level	confidence level to be used for constructing the confidence regions; default is $0.95$ .	
colors	a string vector for the name(s) specifying color(s) to be used for drawing con- fidence regions. If specified, the dimension of the vector needs to be equal the number of considered points (each point corresponds to a set of values for the covariates).	
xlims,ylims	numeric vectors of dimension 2, giving the limits for x and y axes in the plot.	
size_point, size_path		
	numeric values, indicating sizes for point(s) and line(s) in the plot.	
names_labels	an optional character vector giving the label name for covariates.	
nrow_legend	an optional number of rows in the legend.	
file_name	File name to create on disk.	
	further arguments used with ggexport function, for example, width, height.	

# Details

plot.clus\_opt\_thres3 provides plots of confidence regions (and point estimates) of covariate-specific optimal pair of thresholds. The plots are based on ggplot().

# Value

plot.clus\_opt\_thres3 returns plots of confidence regions of covariate-specific optimal pair of thresholds.

# See Also

clus\_opt\_thres3

20

print.ci\_clus\_vus Print summary results from ci\_clus\_vus

#### Description

print.ci\_vus displays the results of the output from ci\_clus\_vus.

# Usage

```
## S3 method for class 'ci_clus_vus'
print(x, digits = 3, ...)
```

# Arguments

Х	an object of class "ci_clus_vus", a result of ci_clus_vus call.
digits	minimal number of significant digits, see print.default.
	further arguments passed to print method.

# Details

print.ci\_clus\_vus shows a summary table for confidence interval limits for covariate-specific VUS.

# Value

print.ci\_clus\_vus shows a summary table for confidence intervals for covariate-specific VUS.

#### See Also

clus\_vus

print.clus\_lme Print summary results of an clus\_lme object

# Description

print.clus\_lme displays results of the output from clus\_lme.

# Usage

```
## S3 method for class 'clus_lme'
print(x, digits = max(3L, getOption("digits") - 3L), call = TRUE, ...)
```

# Arguments

Х	an object of class "clus_lme", a result of clus_lme call.
digits	minimal number of significant digits, see print.default.
call	logical. If set to TRUE, the matched call will be printed.
	further arguments passed to print method.

### Details

print.clus\_lme shows a summary table for the estimated parameters in the cluster-effect model (continuous diagnostic test in three-class setting).

#### Value

print.clus\_lme returns a summary table for the estimated parameters in the cluster-effect model.

# See Also

clus\_lme

print.clus\_opt\_thres3 Print summary results from clus\_opt\_thres3

# Description

print.clus\_opt\_thres3 displays the results of the output from clus\_opt\_thres3.

# Usage

## S3 method for class 'clus\_opt\_thres3'
print(x, digits = 3, call = TRUE, ...)

#### Arguments

х	an object of class "clus_opt_thres3", a result of clus_opt_thres3 call.
digits	minimal number of significant digits, see print.default.
call	logical. If set to TRUE, the matched call will be printed.
	further arguments passed to print method.

# Details

print.clus\_opt\_thres3 shows a summary table for covariate-specific optimal pair of thresholds estimates.

#### Value

print.clus\_opt\_thres3 returns a summary table for results of covariate-specific optimal pair of thresholds estimation.

print.clus\_tcfs

# See Also

clus\_opt\_thres3

print.clus\_tcfs Print summary results from clus\_tcfs

# Description

print.clus\_tcfs displays the results of the output from clus\_tcfs.

# Usage

## S3 method for class 'clus\_tcfs'
print(x, digits = 3, call = TRUE, ...)

# Arguments

х	an object of class "clus_tcfs", a result of clus_tcfs call.
digits	minimal number of significant digits, see print.default.
call	logical. If set to TRUE, the matched call will be printed.
	further arguments passed to print method.

# Details

print.clus\_tcfs shows a summary table for covariate-specific TCFs estimates.

#### Value

print.clus\_tcfs returns a summary table for covariate-specific TCFs estimates.

# See Also

clus\_tcfs

print.clus\_vus

# Description

print.clus\_vus displays the results of the output from clus\_vus.

# Usage

## S3 method for class 'clus\_vus'
print(x, digits = 3, call = TRUE, ...)

# Arguments

х	an object of class "VUS", a result of clus_vus call.
digits	minimal number of significant digits, see print.default.
call	logical. If set to TRUE, the matched call will be printed.
	further arguments passed to print method.

# Details

print.clus\_vus shows a summary table for covariate-specific VUS estimates, containing estimates, standard errors, z-values and p-values for the hypothesis testing  $H_0: VUS = 1/6$  versus an alternative  $H_A: VUS > 1/6$ .

# Value

print.clus\_vus returns a summary table for covariate-specific VUS estimates.

#### See Also

clus\_vus

# Index

```
* data
    data_3class, 16
    data_3class_bcx, 17
    EnergyEthiopia, 17
    MouseNeurons, 18
* package
    ClusROC-package, 3
ci_clus_vus, 4, 21
clus_lme, 3, 5, 8, 11, 13–15, 19, 21, 22
clus_opt_thres3, 3, 8, 20, 22, 23
clus_roc_surface, 3, 10
clus_tcfs, 3, 12, 23
clus_vus, 3–5, 14, 21, 24
ClusROC (ClusROC-package), 3
ClusROC-package, 3
data_3class, 16
data_3class_bcx, 17
EnergyEthiopia, 17
ggexport, 19, 20
integrate, 15
1me, 6
MouseNeurons, 18
na.fail.6
plot.clus_lme, 19
plot.clus_opt_thres3, 19
print, 21-24
print.ci_clus_vus, 21
print.clus_lme, 21
print.clus_opt_thres3, 22
print.clus_tcfs, 23
print.clus_vus, 24
print.default, 21-24
```

```
terms, 7
```